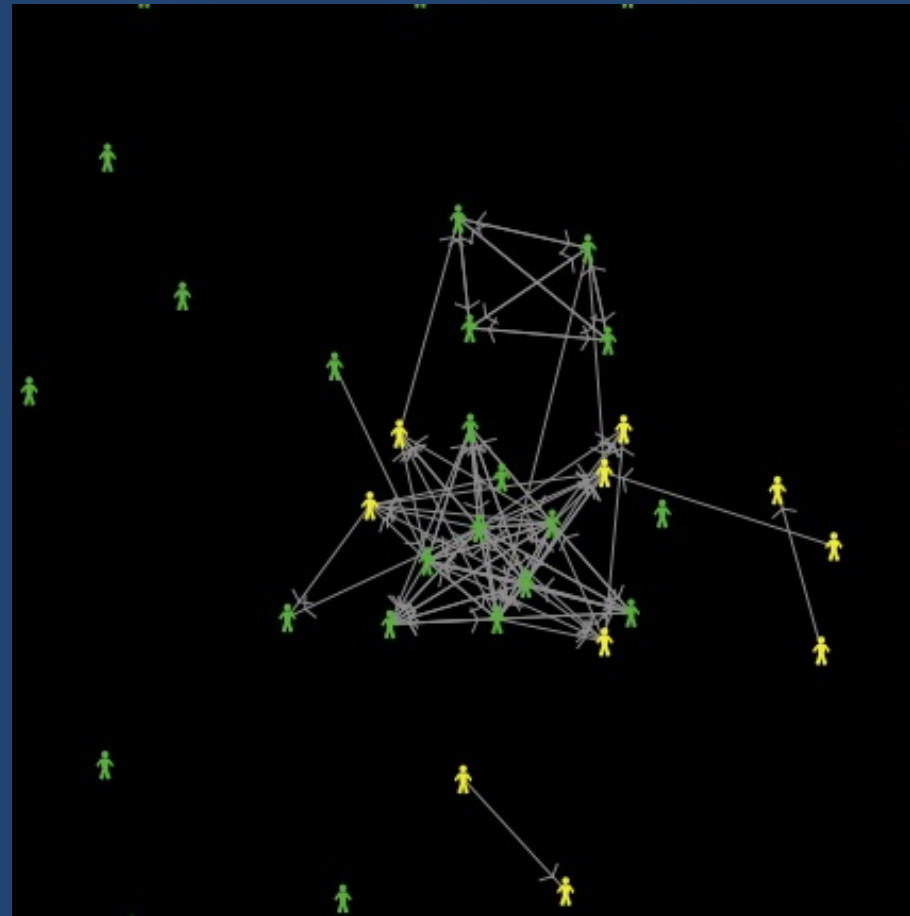


# *Investigating Network Formation Mechanisms with Agent-Based Models*

***Francesco Renzini***

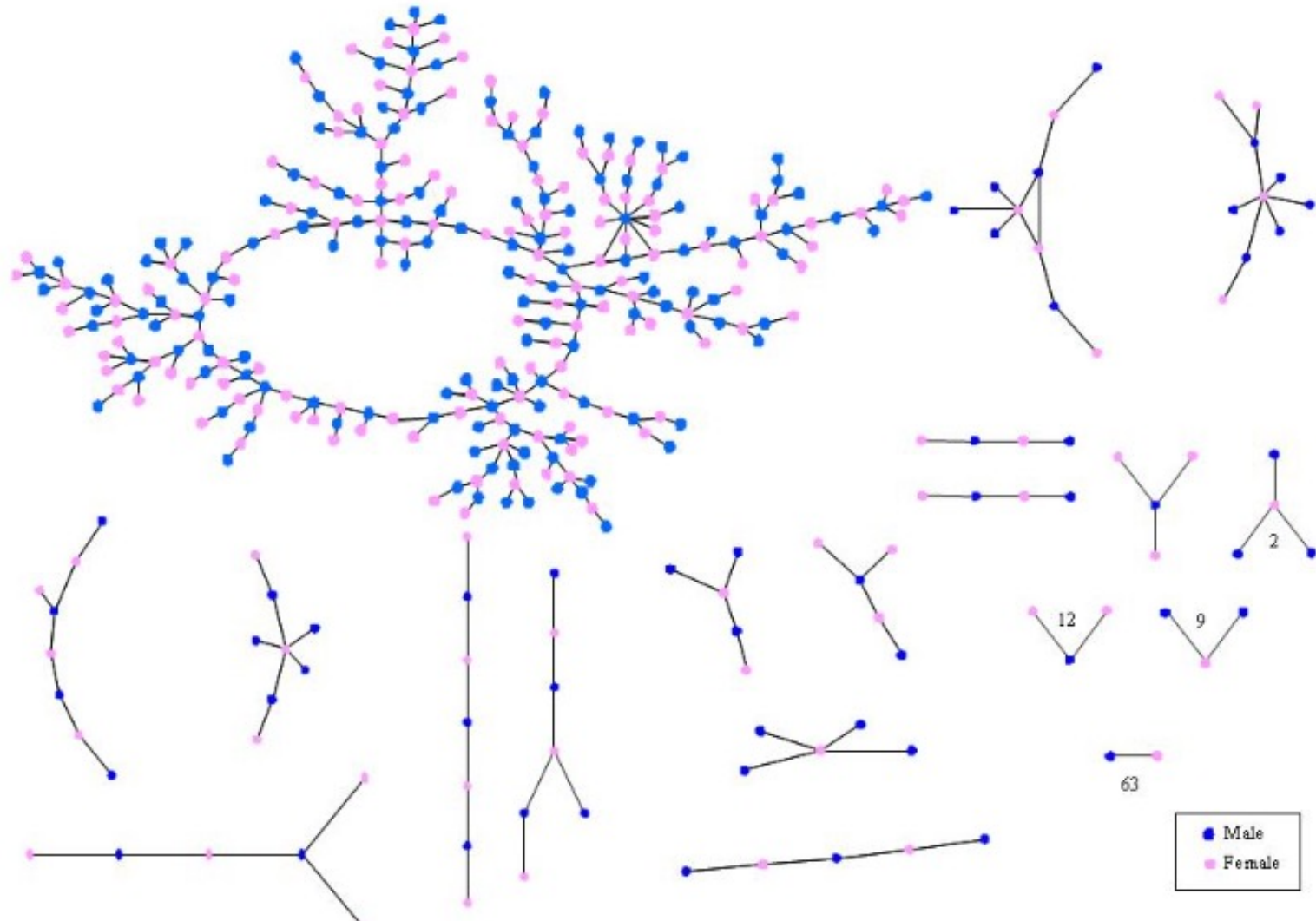
*francesco.renzini@unimi.it*

Department of Social and Political  
Sciences, University of Milan  
Behave Lab



# Bearman et al. (2004): Chains of affection

*Would you care to know the causes behind this structure?*



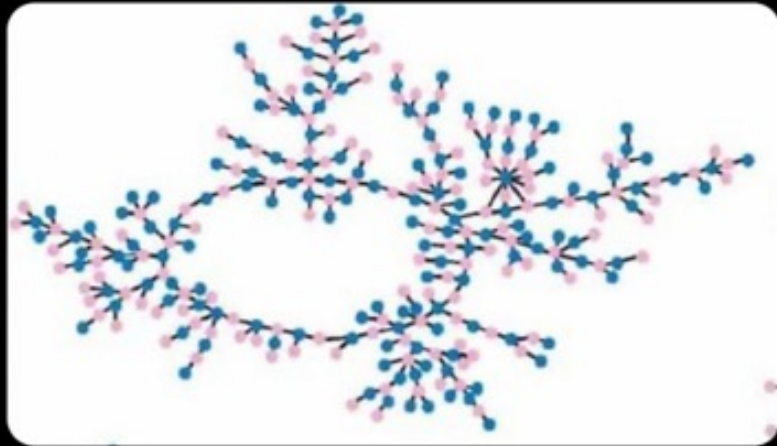


metakuna (13/100 bl...  
@metakuna

Segui

I've just realized how bizarre this is. At first you think "oh these are just the slutty people", but actually the max number of partners for ppl in the actual ring is only 4. They just somehow formed this massive structure with no cross connections???

[Traduci post](#)



15:23 · 16 gen 24 · 678K Visualizzazioni

321 repost 102 citazioni 8.914 Mi piace

1.277 segnalibri

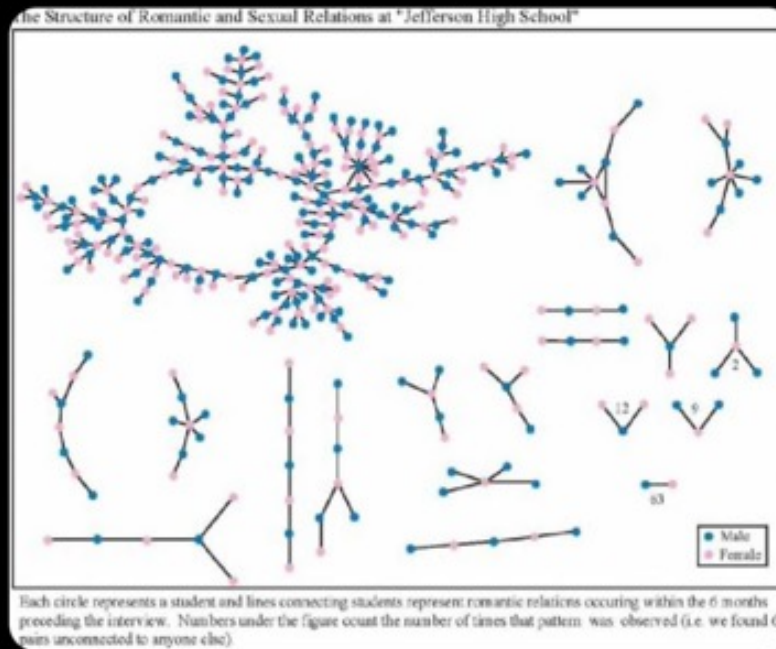


metakuna (13/100 bl...  
@metakuna

Segui

There are like 40 hops! And no smaller ring-like structures in the rest of the network! Why???

[Traduci post](#)



15:23 · 16 gen 24 · 76,6K Visualizzazioni

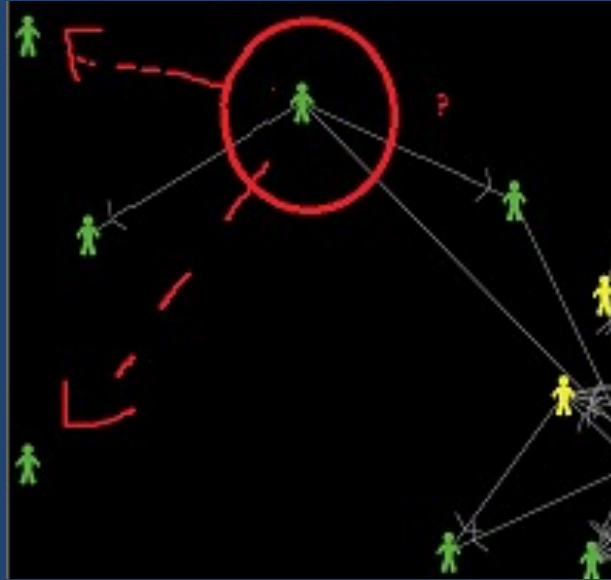
22 repost 8 citazioni 1.670 Mi piace

71 segnalibri



# Networks are complex and fascinating objects

- Outcome of behavior: *Network formation*



- Networks important determinants of many phenomena



# We have a huge problem

- *Determinants behind the selection of network partners are rarely observed → Data scarcity on network formation behavior*
- Need to fill-in these gaps by proposing an explanation for the patterns you observe



- ABM: Help us to compare alternative explanations on common grounds and say something about the phenomenon of interest in case of data scarcity



*How to do so in practice?*









# Social Networks

Volume 76, January 2024, Pages 150-159

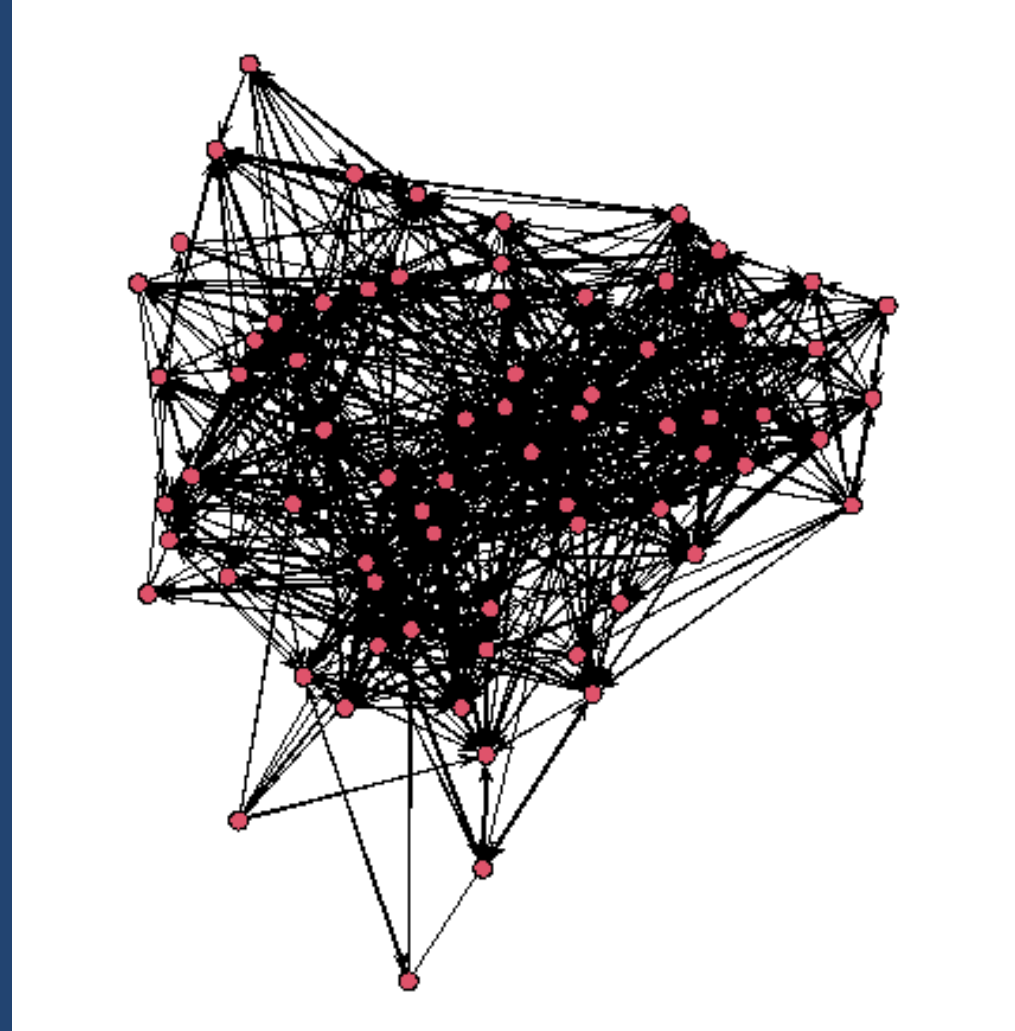


## Status, cognitive overload, and incomplete information in advice-seeking networks: An agent-based model

Francesco Renzini  , Federico Bianchi , Flaminio Squazzoni 



# Context: Lazega (2001)





# The puzzle

- Asking for advice is costly → Status loss
- If status is so important, why do people engage extensively in such a costly activity as advice?
- What network formation mechanism explains the emergence of such network patterns?
- Determinants of network formation were not measured; only the network and some characteristics of lawyers

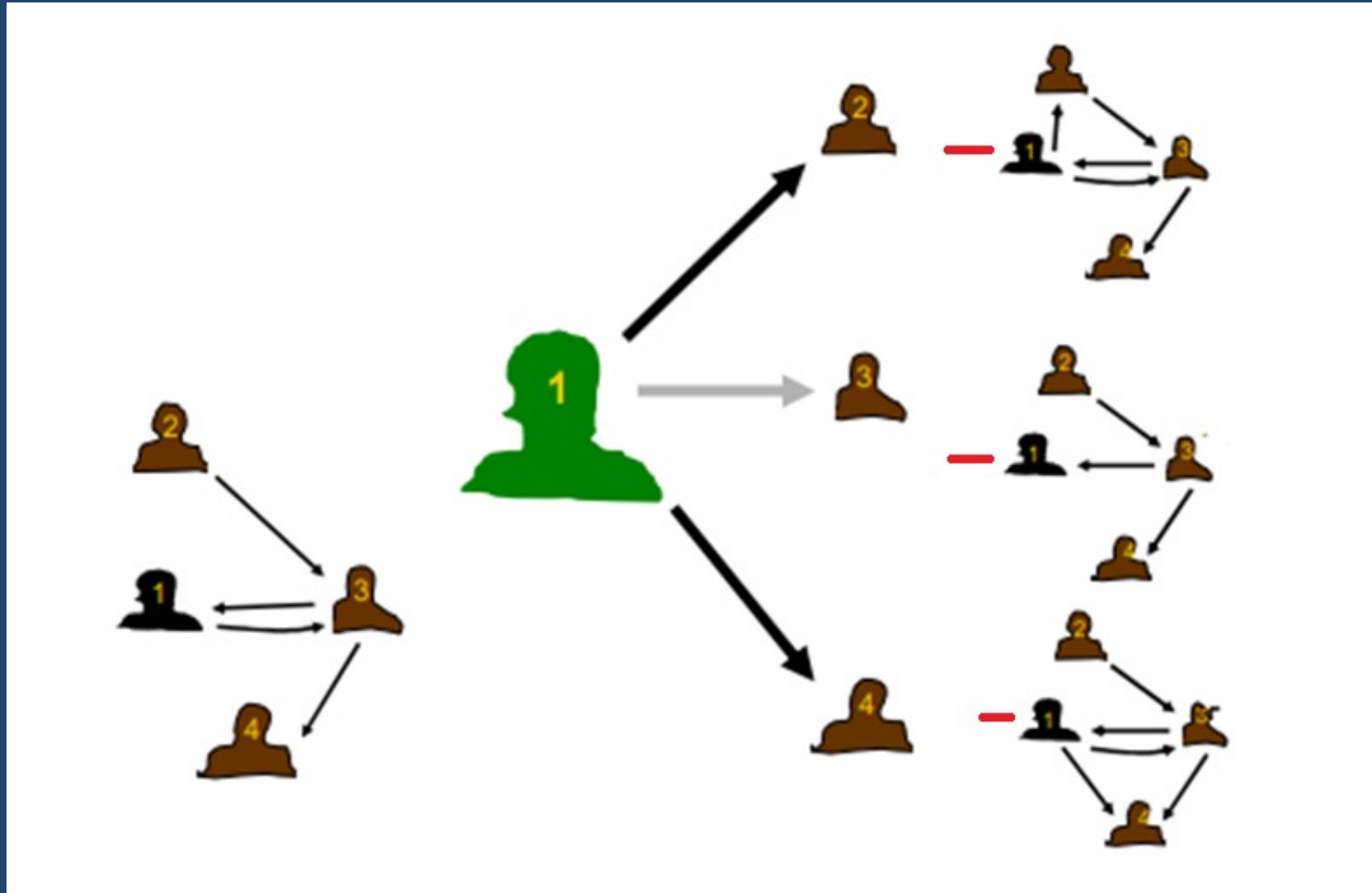


# Fill in the gaps: We need a model

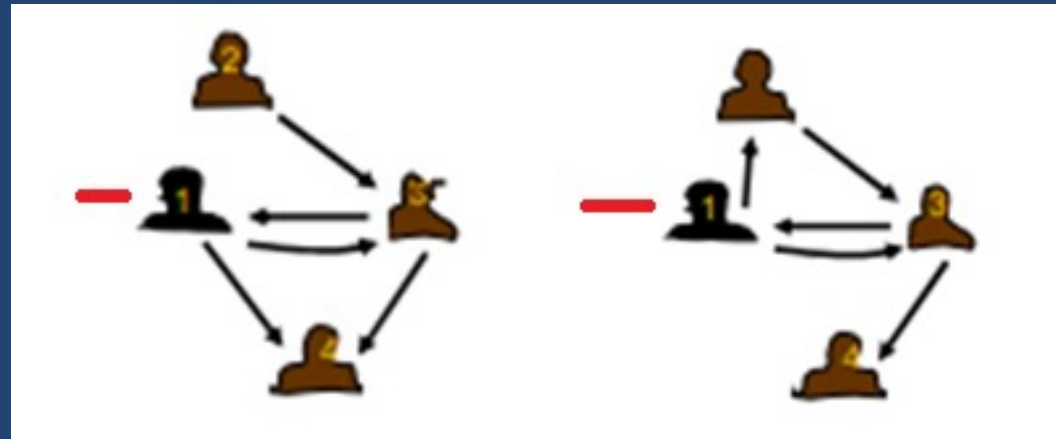
- Stochastic Actor Oriented Models (SAOM; Snijders, 2017; Snijders and Steglich, 2015)
- Simulation-based inference → infer/extract network formation behavior from network data (from the footprints)
- We were not satisfied by the conclusions generated with this approach
- Use ABM to build an alternative theory explaining Lazega's (2001) network
- *This comparison between SAOM and ABM on common grounds (Lazega's network) → Get important insights even if no network formation data*



# SAOM (Snijders and Koskinen, 2010)



# SAOM (Snijders and Koskinen, 2010)

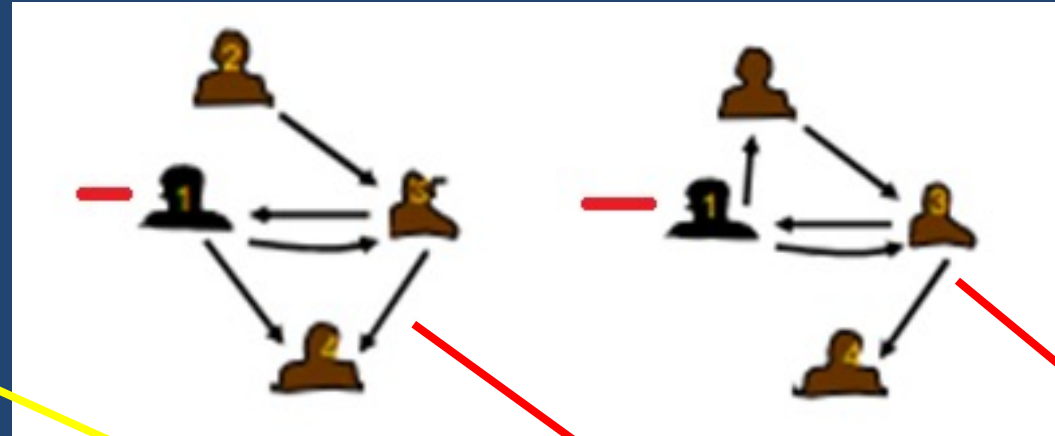


- Local network configurations → Represent network formation behavior (e.g., local hierarchy Vs. generalized exchange)
- Alternatives → Traded off: via objective function = Satisfaction with structure of new state
- Resulting networks will be evaluated in terms of which local configurations arise → Choose the ones we like



# SAOM (Snijders and Koskinen, 2010)

Preferences

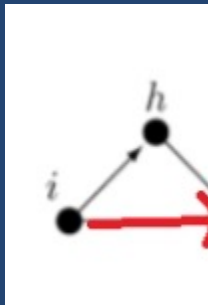


$$f_i(x) = \beta_1 \sum_j x_{ij} + \beta_2 \sum_j x_{ij}x_{ji} + \beta_3 \sum_{j,h} x_{ih}x_{hj}x_{ij} + \beta_4 \sum_{j,h} x_{ih}x_{hj}x_{ji}.$$



# SAOM Approach: Infer NFB from Data

- Specify many local configurations → reflecting many potential and concurrent network formation behaviors (or combinations of behaviors)



## rsiena

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open issues [7](#)    downloads [2k](#)    lifecycle [stable](#)



- Which p... data; ac...
  - Final pr... (hence... network
- SIENA is a program for the statistical analysis of network data, with the focus on social networks. Networks here are understood as entire (complete) networks, not as personal (egocentered) networks: it is assumed that a set of nodes (social actors) is given, and all ties (links) between these nodes are known - except perhaps for a moderate amount of missing data. The name SIENA stands for Simulation Investigation for Empirical Network Analysis. The R package is called RSiena.

- Give ingredients, search algorithm will tell us how to combine them to match data

03/04/24

# Issues with the approach

- Agents are required to perform too demanding calculations, having complex combinations of network formation behaviors **COMPLEX**

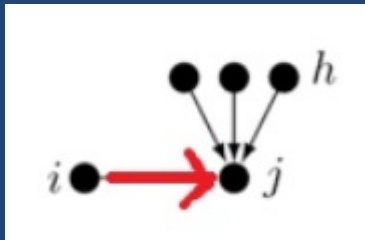
$$f_i(x) = \beta_1 \sum_j x_{ij} + \beta_2 \sum_j x_{ij}x_{ji} + \beta_3 \sum_{j,h} x_{ih}x_{hj}x_{ij} + \beta_4 \sum_{j,h} x_{ih}x_{hj}x_{ji} + \beta_5 \sum_j x_{ij} \sum_h x_{hj} + \beta_6 \sum_j x_{ji} \sum_h x_{jh} + \beta_7 \sum_j x_{ij} \sum_h x_{ih}$$

**Table 11.** Model 5 for Advice Relations: Including also the GWESP Representation of Transitive Closure.

Effect	Parameters	(SE)
Out-degree	-1.745	(0.168)
Reciprocity	1.054	(0.128)
Transitive triplets	0.121	(0.016)
Three cycles	-0.055	(0.028)
In-degree—popularity	-0.011	(0.008)
Out-degree—popularity	-0.062	(0.013)
Out-degree—activity	-0.021	(0.005)
GWESP ( $\alpha = .69$ )	2.045	(0.272)
Seniority receiver	-0.002	(0.003)
Seniority sender	0.009	(0.003)
Seniority similarity	1.110	(0.197)
Seniority of indirect ties	-0.004	(0.002)

Note: GWESP = geometrically weighted edgewise shared partners.

- Supposed to have complete network info



- Not dealing with thresholds/tipping points



**TIED TO DATA**

# Develop an alternative explanation

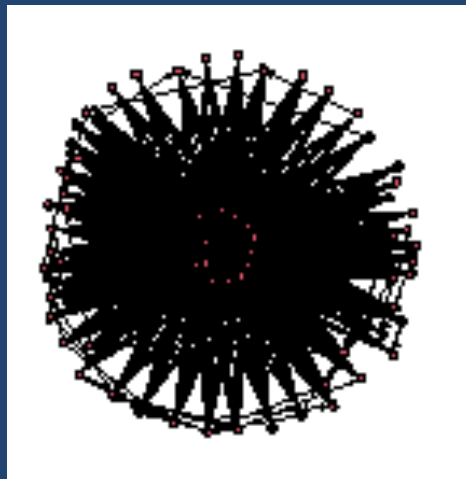
- More empirically plausible agent network formation behavior → delve in advice-networks literature and build from there
- Say something about advice formation by comparing the two approaches





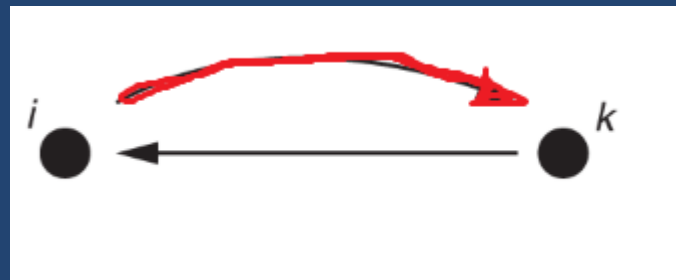
# Our model

- Keep same SAOM structure: Agents max. objFun  $\rightarrow$  change the local configurations
- Every agent has a baseline tendency to seek for advice
- Tendency differs depending on skills, which are unevenly distributed  $\rightarrow$  Low skilled ask to high-skilled
- This might help us to explain centralization (few, attractive high skilled agents) and density (a lot of low skilled, very needy)
- Indeed:

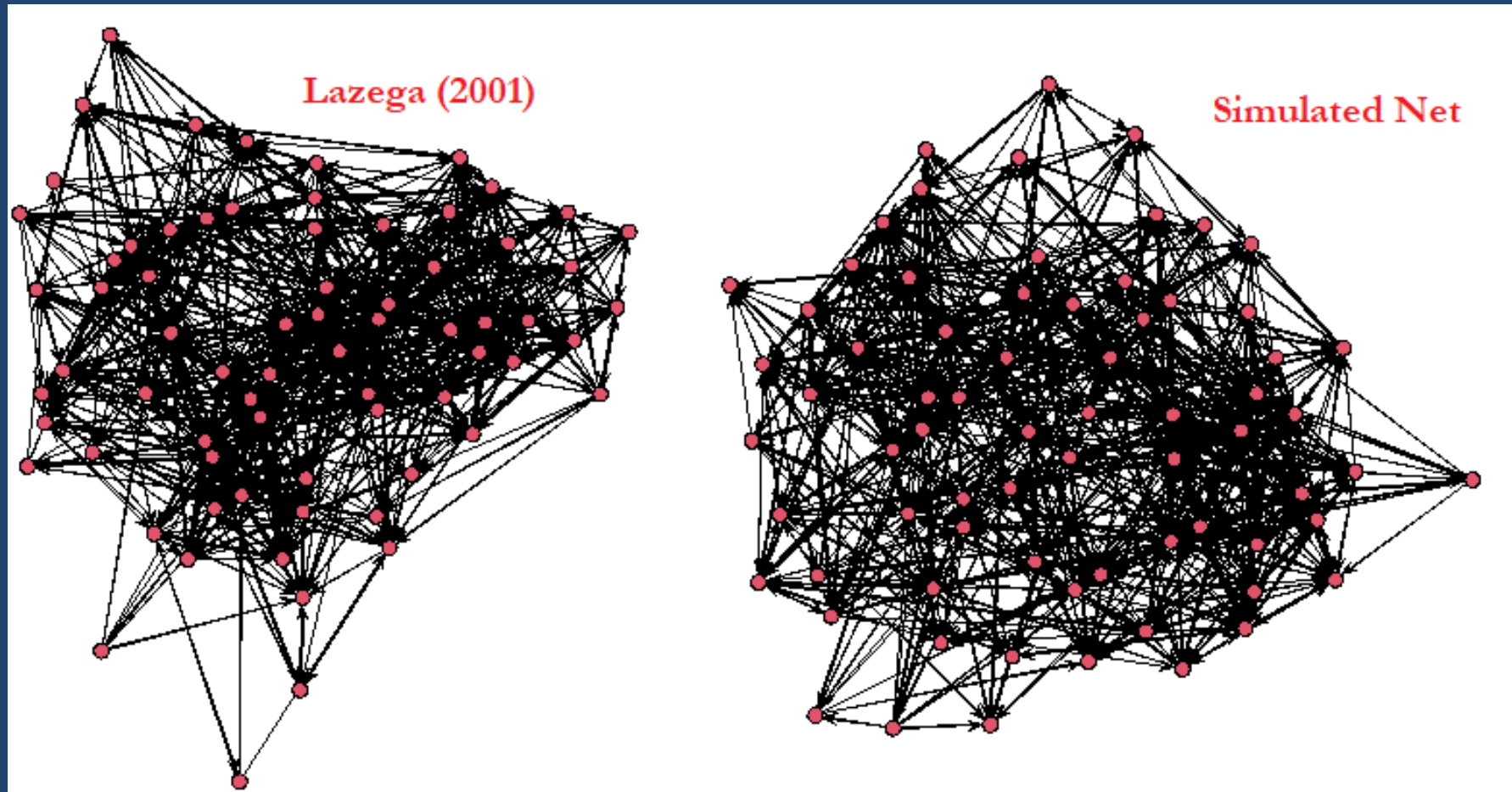


# Our model

- High-skilled agents are easily overloaded; observed also in real world organizations (Lazega et al., 2006; Cross and Prusak, 2016)
- Introduce  $\tau$ , limiting #of incoming requests for the High-skilled
- Low-skilled individuals must find alternative ways to compensate for this information loss  $\rightarrow$  Exploitation (minimize status loss)



# Our model



# Parameters Search

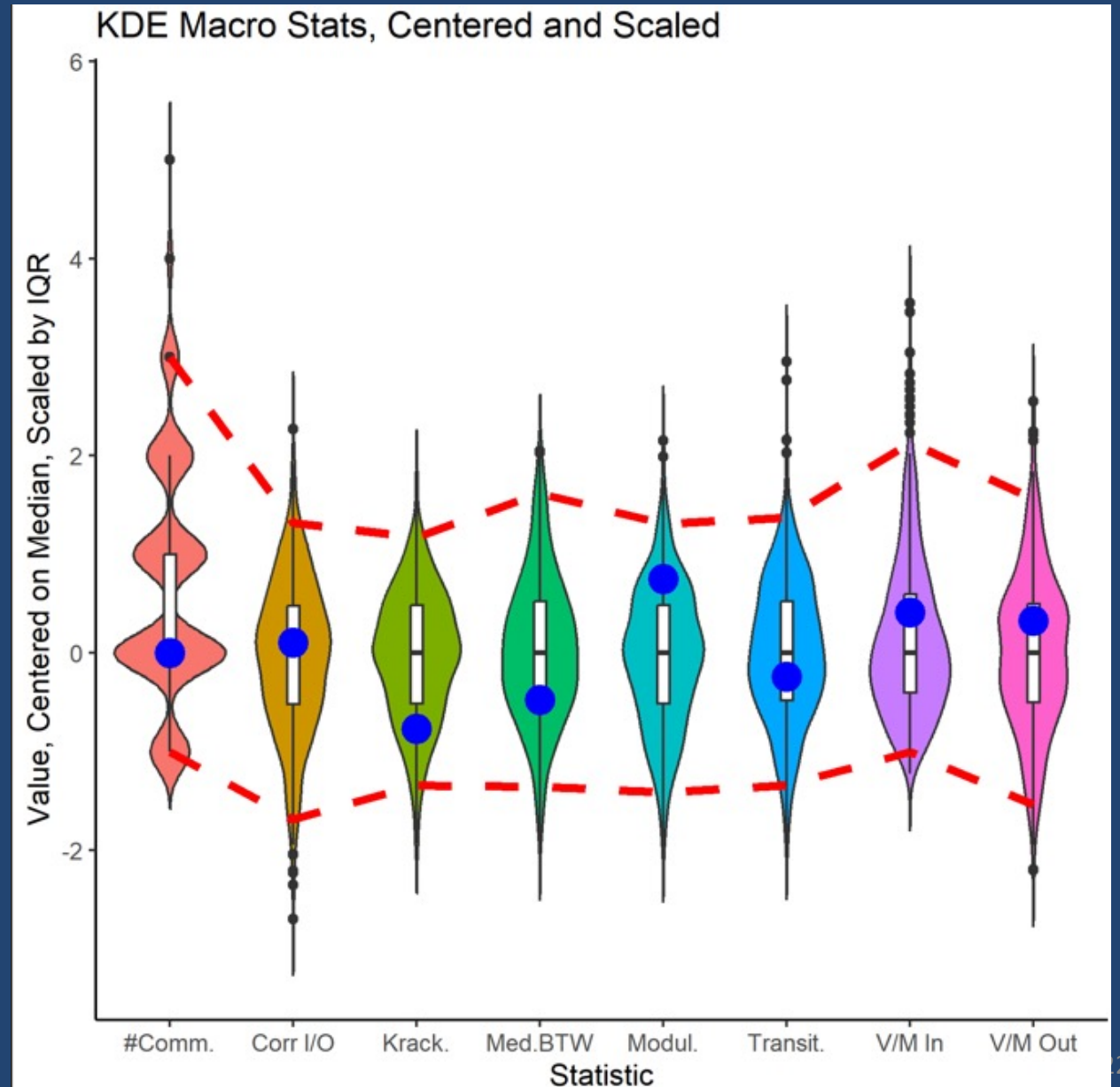
- #of high-skilled,  $\tau$ , and the  $\beta_s$ : attractiveness from low to high, and from high to high, baseline tendencies to seek for advice, exploitation (when redirecting)
- Define plausible intervals (e.g.,  $\tau$  should not be 1 or 40, should be an integer)
- Form a grid, list of unique combinations of plausible parameters
- Run each element of the grid 500 parallel times, compare distributions of simulated networks with Lazega (2001) under specific metrics



# Our model – Empirical Validation

Plus 5 additional other metrics:

- i) #components
- ii) Comp. Size
- iii) G50
- iv) Diameter
- v) #of agents per community



# To sum up – Our model

- Advice networks are the spontaneously emerging “nervous systems” of organizations
- In competitive contexts, it is puzzling to observe dense and complex networks, since asking for advice is costly in terms of status
- Previous research: SAOM
- Our approach: Same contexts, same network, different assumptions, show *another empirically plausible advice formation model*
- *Guide future steps, to say something more about the phenomenon: E.g., search for thresholds (measure them)*
- *Exclude complex network formation behaviors? Say something, even when data is scarce or absent*



# *How to actually implement an ABM?*



25/07/2023

# ABM: Building Blocks

- **Agents** (nodes of the network) → can have various attributes, either observed or not (e.g., in Lazega we observed seniority, but we augmented the dataset with skills and  $\tau$ ) → **Correlation?**
- **Scheduling algorithm**: decide who is acting and when (e.g., which agent can send or withdraw an outgoing link)
- **Decision making algorithm**: how to select advisor (in SAOM framework, objective function, linear combination of network configurations)
- **Conditionals or switches**: what happens in case a condition is satisfied (If any)(ex: triggered a threshold)
- **Routine to estimate parameters and summary statistics for validation**





# Building blocks $\rightarrow$ Algorithms

**Algorithm 2** Network formation from status preferences and cognitive overload

**Require:**  $N > 0$  (number of agents);  $\alpha$  (% of high-skilled agents);  $\tau$  (cognitive overload threshold);  $\beta_0^l, \beta_0^h, \beta_{attract}^l, \beta_{attract}^h, \beta_{EL}^l, \beta_{ER}^l, \epsilon$  (preferences and disturbance);  $T$  (number of iterations)

$t \leftarrow 0$

$G = (N, \emptyset)$   $\triangleright$  Initialize an empty network, with  $N$  nodes, agents  
Determine who is high-skilled from data (if available) or randomly  
Assign  $\tau$  to high-skilled agents

**while**  $t \leq T$  **do**

$l \leftarrow \text{Rand}(1, N)$   $\triangleright$  Randomly select an agent

**if**  $l$  is low-skilled ( $l$ ) **then**

Evaluate  $f_i^l(\beta, X)$  for each  $j \neq i$  and for the do-nothing case

Pick  $j$  that maximizes  $f_i^l(\beta, X)$ , consider to do-nothing

**if**  $j$  is high-skilled and In-Degree ( $j$ )  $> \tau$  **then**

Remove and redirect between 1 and  $\tau$   $l$ -agents asking to  $j$

**for** Every redirecting low-skilled  $l$  **do**

Evaluate low-skilled agents via third term of Eq. (4)

Pick  $j$  that maximizes  $f_i^l(\beta, X)$ , consider to do-nothing

Set  $x_{ij}$  to  $x_{ij}^\pm$ , if best option is to add or remove a link

**end for**

**else**

Set  $x_{ij}$  to  $x_{ij}^\pm$ , if best option is to add or remove a link

**end if**

**else if**  $l$  is high-skilled ( $h$ ) **then**

Evaluate  $f_i^h(\beta, X)$  for each  $j \neq i$  and for the do-nothing case

Pick  $j$  that maximizes  $f_i^h(\beta, X)$ , consider to do-nothing

Set  $x_{ij}$  to  $x_{ij}^\pm$ , if best option is to add or remove a link

**end if**

$t \leftarrow t + 1$

**end while**



# Algorithms → Computer code

Use languages Optimized for OOP (Python, C++, Java, Scala) or Agent-based languages (NetLogo, Repast) → Easier and cleaner to embed in further code for analysis, parameters exploration/estimation

$G = (N, \emptyset)$       ▷ Initialize an empty network, with  $N$  nodes, agents  
Determine who is high-skilled from data (if available) or randomly



## Social Networks

Volume 17, Issue 1, January 1995, Pages 1-26





ated

### Actors and networks as objects ☆

```
if type_  
  attr  
  attr  
  max_  
  if v
```

[Norman P. Hummon](#) , [Thomas J. Fararo](#)

Show more ▾

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[https://doi.org/10.1016/0378-8733\(94\)00245-6](https://doi.org/10.1016/0378-8733(94)00245-6) ↗

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```
g("low"), "Hold"
```

```
shold"][max_index]:
```



# Computer code → Run experiments

```
import gridSearch as gr
import os

os.chdir('') #place here YOUR directory, where you will see the edgelist

#Define combinations of parameters to investigate as a dictionary, where key:param_name, value:list of values to explore

exp = gr.ABMSweeps(**{'N': [71], 'alpha': [0.30, 0.70], 'tau':[15], 'outdeg_l':[-1], 'outdeg_h':[-3],
                    'beta_attr_high':[2.5], 'beta_exploit_low':[1.0], 'beta_explor_low':[0.3, 0.8],
                    'epsilon_location':[0], 'epsilon_scale':[0.3], 'nu_location':[0], 'nu_scale':[0.3],
                    'change_factor_attract':[1]})

#Set up grid of experiment; grid = Cartesian product of parameters
grid_exp = exp.set_up_grid()

nets_to_generate = 100 #for each parameters' combination we generate 100 networks
t = 0
T = 200
path_where_to_save_ts = '' #place here YOUR directory path, in which you want to write time series in .csv
edges_to_stop = 20

results_exp = exp.grid_search(nets_to_generate, t, T, stopping_condition = edges_to_stop, compute_all = True, path_ts =
path_where_to_save_ts)
```



# Run experiments → Estimate parameters

```
with pm.Model() as my_model:  
    exploit = pm.Normal("beta_exploit", mu=0, sigma=3)  
    tau = pm.HalfNormal("tau", sigma=1)  
    s = pm.Simulator("s", NetEvolution, params=(exploit, tau), \  
                    sum_stat="lazega_metrics", epsilon=2, observed=lazega_net)  
    idata = pm.sample_smc()  
    idata.extend(pm.sample_posterior_predictive(idata))
```



# NetLogo – Pedagogical tool

File Edit Tools Zoom Tabs Help

Interface Info Code

Edit Delete Add  normal speed  view updates ticks: 3297  Settings...

setup step iterate

max-links 300 possible-number-links 1560

N 40 number-networkers 30

#satisficers (breed1) #networkers(breed2) #parameters for Gamma distr. of shocks

beta\_outdeg\_sat -1.1 beta\_outdeg\_net -1 alpha 0.2

beta\_hom1\_sat 0.4 beta\_rec\_net 0.9 zeta 2

beta\_attract\_seniority 0.008 beta\_trans\_net 0.7

attr gender

[GitHub Link](#)



# A growing collection of resources for computational model-based science.

AN INTERNATIONAL COMMUNITY AND CYBERINFRASTRUCTURE TO SUPPORT TRANSPARENCY AND REPRODUCIBILITY FOR COMPUTATIONAL MODELS & THEIR DIGITAL CONTEXT + EDUCATIONAL RESOURCES AND FAQ'S FOR AGENT BASED MODELING

Browse the Model Library

## Top Repositories



Find a repository...

- ceco51/Status-hierarchy-cognitive-overload-and-incomplete-network-information-in-advice-seeking-networks-
- ceco51/Evolutionary-network-formation
- ceco51/SIENA-like-model-BEHAVE-SummerSchool
- ceco51/Brokerage
- ceco51/ABM-Peer-Review-NK-
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pyscript / pyscript

### PyScript NEXT (new core) Tech-Preview Release!!

Announcement: PyScript NEXT (new core) Tech-Preview Release!!

After invaluable community feedback, many experiments in code, and careful cooperation with valued collaborators, we are thrilled to announce the tech preview of the new version of PyScript. This work marks a significant milestone in our journey towards PyScript's vision and what our commun...

Read more

## Latest changes

- Yesterday Migrate Bitbucket Server and Data Center repos to GitHub.com (public beta)
- Yesterday GitHub Actions: Removal of Node12 from the Actions runner
- 4 days ago GitHub Copilot July 14th Update
- 4 days ago Codespaces Port Forwarding Domain Name Updates
- View changelog →



Thanks! Any questions?

Contact me: [francesco.renzini@unimi.it](mailto:francesco.renzini@unimi.it)

Twitter: @FrancescoRenz27

